

# Digital sequences with best possible order of $L_2$ discrepancy

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We consider the  $L_2$  discrepancy of digital  $(0,1)$ -sequences over  $\mathbb{Z}_2$  and give conditions on the generator matrix of such a sequence which guarantee minimal possible order of  $L_2$  discrepancy of the generated sequence. We prove for the first time the existence of digital  $(0,1)$ -sequences over  $\mathbb{Z}_2$  with  $L_2$  discrepancy of order  $\sqrt{\log N}/N$ . This order is best possible by a result of K. Roth. Our existence proof is constructive.

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